

Cu₂O(SO₄), Dolerophanite: Refinement of the Crystal Structure, with a Comparison of [O Cu(II)₄] Tetrahedra in Inorganic Compounds

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The refinement of the crystal structure of Cu₂O(SO₄), dolerophanite, [$a = 9.370(1) \text{ \AA}$, $b = 6.319(1) \text{ \AA}$, $c = 7.639(1) \text{ \AA}$, $\beta = 122.34(1)^\circ$; space group C 2/m; $Z = 4$; $R = 0.035$] confirmed the trigonal dipyramidal coordination of one Cu(II) atom (mean distance Cu—O = 2.025 Å). One O atom is tetrahedrally surrounded by four Cu(II) atoms; the mean Cu(II)—O distance of 1.918 Å compares well to [O Cu(II)₄] tetrahedra found in inorganic crystal structures.

[Keywords: Cu₂O(SO₄); Dolerophanite; Crystal structure refinement; [O Cu(II)₄] Tetrahedron]

Cu₂O(SO₄), Dolerophanit: Verfeinerung der Kristallstruktur mit einem Vergleich von [O Cu(II)₄]-Tetraedern in anorganischen Verbindungen

Die Verfeinerung der Kristallstruktur von Cu₂O(SO₄), Dolerophanit, [$a = 9.370(1) \text{ \AA}$, $b = 6.319(1) \text{ \AA}$, $c = 7.639(1) \text{ \AA}$, $\beta = 122.34(1)^\circ$; Raumgruppe C 2/m; $Z = 4$; $R = 0.035$] bestätigte die trigonal dipyramidale Koordination des einen Cu(II)-Atoms (mittlerer Cu—O-Abstand = 2.025 Å). Ein O-Atom ist tetraedrisch von vier Cu(II)-Atomen umgeben; der mittlere Cu(II)—O-Abstand von 1.918 Å entspricht den in ähnlichen [O Cu(II)₄]-Tetraedern von anorganischen Kristallstrukturen gefundenen Werten.

Introduction

Flügel-Kahler¹ determined the crystal structure of Cu₂O(SO₄), dolerophanite, on natural material and gave a detailed description of the structure type. In connection with studies of the coordination chemistry of Cu(II) atoms a refinement of dolerophanite was performed (a) to confirm the trigonal dipyramidal coordination of one Cu(II) atom, and (b) for a

comparison with $[\text{OCu(II)}_4]$ tetrahedra in inorganic crystal structures. Because of lack of natural crystals synthetic material was used.

Results

Synthesis

Crystals of $\text{Cu}_2\text{O}(\text{SO}_4)$ were synthesized under following conditions: a mixture of $\text{CuSO}_4 \cdot 5\text{H}_2\text{O}$, KHSO_4 , and $\text{CuCl}_2 \cdot 2\text{H}_2\text{O}$ (molecular ratio 1:1:10) was first heated for 2 hours at 150 (5) °C and afterwards for 5 hours at 600 (10) °C in a china crucible at atmospheric pressure. After a cooling-off period of ~12 hours the compounds $\text{Cu}_2\text{O}(\text{SO}_4)$ and $\text{K}_4[\text{Cu}_2\text{O}(\text{SO}_4)_2]_2 \cdot \text{KCl}$ (cf. caratiite²) were obtained. The needle-like crystals of the title compound are yellowish brown in colour (elongated parallel to [010]).

Refinement of the Crystal Structure

For the crystal data as well as for the parameters of the data collection cf. Table 1. The X-ray intensities were corrected for absorption (empirical ψ scans) as well as for Lorentz- and polarization effects. The atomic coordinates given in ¹ were used in the starting set of a full-matrix least-squares refinement. Complex scattering functions³ were used, and a secondary isotropic extinction correction was applied⁴. The obtained *R* values are included into Table 1; the structure parameters are given in Table 2; finally the largest difference of an atomic position given in ¹ and in this refinement is 0.06 Å [atom O(2)], the mean value is 0.02 Å.

Table 1. Summary of crystal data, X-ray intensity measurements, and crystal structure refinement for *dolerophanite*

$a = 9.370(1) \text{ \AA}$	STOE four-circle diffractometer and
$b = 6.319(1) \text{ \AA}$	program system STRUCSI on an ECLIPSE S/140
$c = 7.639(1) \text{ \AA}$	graphite monochromatized MoK α radiation
$\beta = 122.34(1)^\circ$	crystal dimensions: 0.025 × 0.09 × 0.04 mm ³
$V = 382.1 \text{ \AA}^3$	scan speed ratio: $2\theta : \omega = 1 : 1$
Temperature: 295 K	step width: 0.03°
space group: C 2/m	steps/reflection: 35 + (α_1, α_2) splitting
$Z = 4 \{ \text{Cu}_2\text{O}(\text{SO}_4) \}$	time/step: 0.5 to 1.5 s
$\mu(\text{MoK}\alpha) = 113 \text{ cm}^{-1}$	3 standard reflections measured each 60 min
	range of data: $3^\circ < 2\theta < 60^\circ$
no. of variables: 47	measured reflections: 1040 ($\pm h - k \pm l$)
$R = 0.035$	unique reflections: 598
$R_w = 0.032$	unique reflections with $F_o > 3\sigma(F_o)$: 558
$w = 1.251/[\sigma(F_o)]^2$	(used for the crystal structure refinement)

Table 2. Atomic coordinates and anisotropic temperature parameters for dolerophanite with e.s.d.'s in parentheses.

$$ATF = \exp[-2\pi^2 \sum_{i=1}^3 \sum_{j=1}^3 U_{ij} a_i^* a_j^* h_i h_j]$$

Atom	Wyckoff notation	Site symmetry	x/a	y/b	z/c	U _{equiv}
Cu(1)	4e	1	1/4	1/4	0	0.009
Cu(2)	4i	m	0.0721 (1)	0	0.2182 (1)	0.010
S	4i	m	0.1024 (2)	1/2	0.3157 (3)	0.008
O(1)	4i	m	0.2038 (7)	1/2	0.2232 (9)	0.019
O(2)	4i	m	0.2947 (6)	0	0.4593 (8)	0.014
O(3)	4i	m	0.1514 (5)	0	0.0217 (7)	0.008
O(4)	8j	1	0.4916 (4)	0.1906 (6)	0.2498 (5)	0.012

Atom	U ₁₁	U ₂₂	U ₃₃	U ₁₂	U ₁₃	U ₂₃
Cu(1)	0.0055 (4)	0.0106 (4)	0.0138 (4)	—	0.0025 (3)	0.0023 (3)
Cu(2)	0.0050 (4)	0.0175 (5)	0.0088 (4)	0	0.0002 (3)	0
S	0.0060 (6)	0.0101 (7)	0.0099 (7)	0	0.0016 (5)	0
O(1)	0.022 (3)	0.028 (3)	0.025 (3)	0	0.017 (3)	0
O(2)	0.008 (2)	0.024 (3)	0.009 (2)	0	—	0
O(3)	0.004 (2)	0.009 (2)	0.010 (2)	0	0.001 (2)	0
O(4)	0.008 (1)	0.010 (2)	0.018 (2)	0.001 (1)	0.000 (1)	0.002 (1)

Discussion

The Cu(1) atom is "square planar" coordinated by O atoms with Cu(1)—O = 1.882(2) Å and 2.070(3) Å ("[CuO₄] square"). The coordination figure is completed to a distorted octahedron by two distant O atoms [2.526(5) Å]. Contrary the Cu(2) atom is trigonal dipyramidal coordinated with only slightly varying Cu(2)—O bond lengths. The mean Cu(2)—O of 2.025 Å is 2.5% longer than the mean value within the [Cu(1)O₄] square. The Cu(2) atom is shifted out of the plane defined by the three equatorial O atoms into the direction of one apex by 0.283 Å. Nevertheless, the bond lengths to both the apexes are equal to each other within one e.s.d. [Cu—O = 1.906(6) Å; 1.907(5) Å], and they are the shortest bonds within the coordination polyhedron of the Cu(2) atom [for the equatorial O atoms Cu—O = 2.000(5) Å; 2.155(3) Å, 2 ×]. Further O atoms have Cu(2)—O ≥ 3.3 Å. Similar coordinations of Cu(II) atoms have been found only in a few inorganic crystal structures (cf. ⁵⁻⁷).

The S—O bond lengths of the [SO₄] group can be correlated with the coordination of the O atoms: S—O(1) = 1.456(6) Å and S—O(2) = 1.453(6) Å are equal to each other within one e.s.d.; the O(1) atom builds two long, the O(2) atom one short Cu—O bond. The O(4) atom builds two short Cu—O bonds [S—O(4) = 1.491(3) Å].

Table 3. Comparison of O atoms coordinated by four Cu(II) atoms in inorganic crystal structures

Chemical formula (mineral name)	O—Cu (in Å)		Cu—O—Cu (in °)
	from-to	mean	
CuO (tenorite) ⁸	1.951-1.961	1.956	95.7-145.8
Cu ₂ O(SO ₄) (dolerophanite)	1.882-2.000	1.918	93.6-117.6
K ₄ [Cu ₂ O(SO ₄) ₂] ₂ ·MeCl (caratiite) ²	1.902-1.948	1.925	97.8-114.7
Cu ₄ O(PO ₄) ₂ ^{9,10}	1.895-1.924	1.911	96.9-142.5
Cu ₅ O ₂ (PO ₄) ₂ ¹¹	1.909-1.943	1.932	95.1-125.0
Cu ₃ Mo ₂ O ₉ ¹²	1.860-1.962	1.899	102.6-135.1

The atom O(3) is tetrahedrally coordinated by two Cu(1) and two Cu(2) atoms. Table 3 gives a survey of inorganic compounds with an O atom coordinated only by Cu(II) atoms. All the coordination polyhedra are more or less distorted tetrahedra. It is to be mentioned that they were only found in compounds without any H₂O molecules or OH groups.

The Cu—O bonds in the different [O Cu(II)₄] tetrahedra summarized in Table 3 represent in most cases (short) bonds within "[CuO₄] squares";

two exceptions are known: in Cu₂O(SO₄) and in Cu₅O₂(PO₄)₄ trigonal dipyramidal coordinated Cu(II) atoms were found which are involved at the building of [O Cu(II)₄] tetrahedra. From the formula given by *Brown* and *Wu*¹³ for calculating bond valences one can calculate a formal O^[4Cu]—Cu(II) distance of 1.93 Å, which compares well to the mean values given in Table 3. The maximum difference of the O—Cu bonds within one [O Cu(II)] tetrahedron was found to be 0.118 Å [in Cu₂O(SO₄)], in total they vary for 0.140 Å [the shortest was found in Cu₃Mo₂O₉, and the longest one in Cu₂O(SO₄) for the Cu(2)^[5] atom]. The Cu—O—Cu bond angles are varying within these coordination polyhedra from 93.6° in Cu₂O(SO₄) to 145.8° in CuO.

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